

# Second Harmonic Scattering as a Probe of Structural Correlations in Liquids

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Second harmonic scattering experiments of water and other bulk molecular liquids have long been assumed to be insensitive to interactions between the molecules. The measured intensity is generally thought to arise from incoherent scattering due to individual molecules. We introduce a method to compute the second harmonic scattering pattern of molecular liquids directly from atomistic computer simulations, which takes into account the coherent terms. We apply this approach to large scale molecular dynamics simulations of liquid water, where we show that nanosecond second harmonic scattering experiments contain a coherent contribution arising from radial and angular correlations on a length-scale of  $\lesssim 1$  nm - much shorter than had been recently hypothesized [1]. By combining structural correlations from simulations with experimental data [1] we can also extract an effective molecular hyperpolarizability in the liquid phase. This work demonstrates that second harmonic scattering experiments and atomistic simulations can be used in synergy to investigate the structure of complex liquids, solutions and biomembranes, including the intrinsic inter-molecular correlations.

Nonlinear light scattering has been widely used to investigate aqueous interfaces, including suspensions of metallic or semiconducting nanoparticles, water droplets and biological membranes (for example, Refs. [2–15]). In particular, second harmonic scattering (SHS), also commonly referred to as Hyper-Rayleigh scattering (HRS; the terms SHS and HRS are used interchangeably in this work), is especially sensitive to the molecular orientation of liquids at interfaces: there is a greater contribution to radiated second harmonic light arising from molecules at the interface, where inversion symmetry is broken, compared to those in the bulk, which is on average centrosymmetric. In bulk liquids the coherent term is usually assumed to be negligible and the measured signal is mostly interpreted in terms of fully incoherent scattering from individual molecules [16, 17]. Under this assumption, the SHS intensity of a solution can be expressed as a linear combination of the incoherent contribution of the solute and of that of the solvent. Using this approach the average hyperpolarizability of a molecule in solution can be estimated [18].

This assumption stems from early work by Terhune *et al.*, who neglected the coherent contribution to the intensity because the wavelength of the laser is much larger than the range of molecular correlations expected in a liquid [16]. Although Bersohn and Maker later developed a theory to include coherent scattering due to structural correlations [19, 20], these additional terms have been largely ignored in the interpretation of experiments. More recently, in a series of articles by Shelton *et al.*, a sign of coherence has been reported from nanosecond HRS measurements on bulk liquids including water and acetonitrile [1, 21–24]. A diverse range of possible origins was suggested for this coherence: a third

order response arising from collective polar modes [21], collective rotation of molecules [22], the presence of ferroelectric domains [23], coupling of rotations and translations in acoustic phonons extending up to 2000 nm [1], or orientational correlations found in ideal isotropic homogeneous random vector fields [24]. Clearly SHS measurements contain information about the intermolecular structure of liquids although it is evident that no consensus has been reached on their origin (see *e.g.* Ref. [25]) and their length scale. So far, experiments in bulk water have been interpreted by treating intermolecular correlations as fitting parameters [1, 24] and a framework to explicitly account for the correlations that give rise to coherent scattering in SHS experiments has not yet been developed. Recent elastic femtosecond SHS measurements from ionic solutions have shown that several different electrolytes induce long-range orientational correlations in water, starting at concentrations as low as 10  $\mu$ M [26]. The strong dependence on isotopic composition also suggests a link between these observations and the H-bond network of water.

The liquid-phase hyperpolarizability plays a crucial role in the interpretation of SHS experiments. Measurements have often been analyzed using a molecular non-linear response tensor of water obtained from quantum chemical calculations [27]. However, the model that underlies the evaluation of the hyperpolarizability in Ref. [27] described the surroundings of a water molecule by three point charges, which does not take into account the many complex molecular environments that can be found in liquid water [28].

In this work we present a method to compute the SHS intensity directly from atomistic computer simulations, including both the incoherent *and* the coherent contri-

butions. This framework is used to calculate the angular scattering pattern from large-scale force-field molecular dynamics (MD) simulations of liquid water. We show that quantitative agreement with nanosecond HRS experiments [1] cannot be achieved by using the values of molecular hyperpolarizability often used to interpret experiments, [27] obtained with Møller-Plesset perturbation theory expanded up to the fourth order (MP4). We find instead that it is possible to obtain satisfactory agreement by combining the correlations obtained from simulations with an effective liquid phase molecular hyperpolarizability, used as a fitting parameter. The values obtained for this hyperpolarizability can be used to provide a more quantitative interpretation of other SHS experiments. By computing explicitly the correlations that contribute to the SHS signal, we can also gather insight into the length scales that are most relevant for these experiments.

We begin by introducing the general expression for the SHS intensity  $I(\mathbf{q}, \mathbf{u}, \mathbf{v})$  for an ensemble of  $N$  molecules at a scattered wave-vector  $\mathbf{q}$  and with the polarization directions of the incoming and outgoing beams defined by the vectors  $\mathbf{u}$  and  $\mathbf{v}$ :

$$I(\mathbf{q}, \mathbf{u}, \mathbf{v}) \propto N^{-1} \left\langle \left| \sum_{\alpha} \beta(\alpha, \mathbf{u}, \mathbf{v}) e^{i\mathbf{q} \cdot \mathbf{r}_{\alpha}} \right|^2 \right\rangle, \quad (1)$$

where the brackets indicate a time average over uncorrelated configurations and  $\beta(\alpha, \mathbf{u}, \mathbf{v})$  is the component of the hyperpolarizability of a scattering unit  $\alpha$  in the laboratory reference frame ( $L$ ) projected onto the polarization direction of the incoming ( $\mathbf{u}$ ) and outgoing ( $\mathbf{v}$ ) beams, *i.e.*  $\beta(\alpha, \mathbf{u}, \mathbf{v}) = \sum_{LMN} \beta_{LMN}^L(\alpha) v_L u_M u_N$ , and the proportionality constant can be found in Ref. [19]. A schematic of the geometric setup is shown in the Supporting Information (SI) in Fig. S1. Eq. 1 can be decomposed into the sum of an incoherent term and of a coherent term respectively [19]:

$$I(\mathbf{q}, \mathbf{u}, \mathbf{v}) \propto N^{-1} \left\langle \sum_{\alpha} \beta(\alpha, \mathbf{u}, \mathbf{v})^2 \right\rangle + N^{-1} \left\langle \sum_{\alpha} \sum_{\alpha' \neq \alpha} \beta(\alpha, \mathbf{u}, \mathbf{v}) \beta(\alpha', \mathbf{u}, \mathbf{v}) e^{i\mathbf{q} \cdot (\mathbf{r}_{\alpha} - \mathbf{r}_{\alpha'})} \right\rangle. \quad (2)$$

The hyperpolarizability in the laboratory frame  $\beta_{LMN}^L$  can be obtained by applying the rotations  $\beta_{LMN}^L = \sum_{abc} \beta_{abc}^M c_{aL} c_{bM} c_{cN}$ , with  $\beta_{abc}^M$  being the molecular hyperpolarizability in the molecular frame and  $c_{iI}$  the projection of the  $i^{\text{th}}$  unit vector in the molecular frame on the  $I^{\text{th}}$  unit vector in the lab frame. In the following we assume that  $\beta_{abc}^M$  can be expressed as an effective molecular hyperpolarizability  $\langle \beta_{abc}^M \rangle$ .

As previously discussed, in bulk liquids the coherent term in Eq. 2 – which describes the interference between the waves scattered by two molecules – would average

to zero if the instantaneous relative orientation of different molecules were completely random, and is often assumed to be negligible compared to the incoherent term [2, 16, 18, 20] In order to test this assumption, we developed a framework to explicitly evaluate Eq. 1 for MD simulations. We applied this framework to MD simulations of liquid water involving about 260,000 molecules, using a cubic simulation box with a side of 20 nm. Simulations were performed with the GROMACS code v.5.0.4 [29], using the rigid TIP4P/2005 water model [30]. The equations of motion were integrated in the NVT ensemble using the velocity Verlet algorithm for 20 ns with a 2 fs timestep. Temperature control was achieved using the stochastic velocity rescaling thermostat [31], with a target temperature of 300 K. Full details of the computational setup can be found in the Supporting Information. We performed extensive tests on the setup to ensure that it was insensitive to finite size effects and the type of force-field used.

Fig. 1 shows the ratios of the SHS intensities of bulk water reported by Shelton in Ref. [1] using nanosecond experiments at different polarization combinations as a function of the scattering angle ( $\theta$ ) and as computed in this work from the analysis of our MD simulations. The convention used for the polarization combinations follows Ref. [26] and references therein. Light polarized parallel to the scattering plane is denoted by P and light polarized perpendicular to the scattering plane is denoted by S. A polarization combination is specified as XYY, with X (= P or S) the polarization of the outgoing beam and Y (= P or S) that of the incoming beam. Fig. 1(a) illustrates the intensity ratios obtained from our simulations under the assumption of purely incoherent scattering. We use the constant hyperpolarizability from Ref. [27], computed using MP4 and modelling a liquid-like environment by placing point charges in a geometry resembling the first solvation shell. Despite its simplicity, this model has been used in several studies of the hyperpolarizability of water [32, 33]. It can be seen that a model for the intensity assuming only incoherent scattering completely fails to account for the qualitative features of the experimental curves, which show an asymmetry with respect to 90 degrees and a varying  $I_{\text{SPP}}/I_{\text{PSS}}$  ratio.

We then proceed to compute the intensity with the full Eq. 1, using the  $\langle \beta_{abc}^M \rangle$  elements from Ref. [27]. As shown in Fig. 1(b), the functional form of the plot extracted from the simulation is markedly different from that of Fig. 1(a) and reproduces the main features of the experimental curves. However, the computed ratios show a clear quantitative difference from the experimental ratios. Rather than trying to refine the evaluation of this effective hyperpolarizability [33–35], one could extract the molecular correlations from the atomistic simulation, and verify whether the experimentally measured intensities can be reproduced by using the values of  $\langle \beta_{abc}^M \rangle$  as fitting parameters.

In order to investigate this point, we reformulate Eq. 1 in a form that separates intermolecular correlations and the tensor elements of the constant effective molecular hyperpolarizability  $\langle\beta_{abc}^M\rangle$  in the liquid phase. We introduce the sixth-order tensor  $W_{abcdef}(\mathbf{q}, \mathbf{u}, \mathbf{v}) = N^{-1} \sum_{\alpha, \alpha'} S_{abc}^*(\mathbf{q}, \mathbf{r}_\alpha, \mathbf{u}, \mathbf{v}) S_{def}(\mathbf{q}, \mathbf{r}_{\alpha'}, \mathbf{u}, \mathbf{v})$ , where,

$$S_{abc}(\mathbf{q}, \mathbf{r}_\alpha, \mathbf{u}, \mathbf{v}) = \sum_{LMN} c_{aL} v_L c_{bM} u_M c_{cN} u_N \exp(i\mathbf{q} \cdot \mathbf{r}_\alpha). \quad (3)$$

$W_{abcdef}(\mathbf{q}, \mathbf{u}, \mathbf{v})$  includes both the single-molecule term giving rise to incoherent scattering and the coherent contribution due to the intermolecular radial and angular correlations. Inserting this expression into Eq. 1 we obtain,

$$I(\mathbf{q}, \mathbf{u}, \mathbf{v}) \propto \sum_{abcdef} \langle\beta_{abc}^M\rangle \langle\beta_{def}^M\rangle \langle W_{abcdef}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle. \quad (4)$$

Because SHS experiments are performed at a value of  $q$  of the order of  $10^{-2} \text{ nm}^{-1}$ , which is too small to be probed in simulations, we extrapolate  $\langle W_{abcdef}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle$  to the  $q \rightarrow 0 \text{ nm}^{-1}$  limit (see SI). Having separated the expression for the intensity into the effective molecular hyperpolarizability and the structural correlation term  $\langle W_{abcdef}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle$ , it is possible to use Eq. 4 to determine the value of  $\langle\beta_{abc}^M\rangle$  that best matches experiments. The  $\langle\mathbf{W}(\mathbf{q}, \mathbf{u}, \mathbf{v})\rangle$  tensor needs to be computed only once, and weighted with tentative values of the hyperpolarizability tensor to find the best fit. Under nonresonant conditions [36], and under the assumption that each water molecule in the condensed phase has  $C_{2v}$  symmetry, there are only three independent components of the molecular hyperpolarizability tensor, *i.e.*  $\beta_{zxx}^M$ ,  $\beta_{zyy}^M$  and  $\beta_{zzz}^M$ . One value of the three elements of the hyperpolarizability is linearly dependent on the other two because most of the time, intensity ratios are extracted from SHS experiments, rather than the bare intensities.

With these hypotheses in place, Fig. 2 shows the error ( $\chi^2$ ) of the fit to the experimental data of Ref. [1] as a function of  $\langle\beta_{zxx}^M\rangle/\langle\beta_{zzz}^M\rangle$  and  $\langle\beta_{zyy}^M\rangle/\langle\beta_{zzz}^M\rangle$ . This plot can be used to ascertain the quality of a given model to compute the effective molecular hyperpolarizability in the condensed phase. For instance, the values of the molecular hyperpolarizabilities in the model of Ref. [27] (the square symbol) give a much larger  $\chi^2$  compared to the best estimate obtained by our fitting procedure (the circle symbol). It can also be seen that the parameter space of  $\langle\beta_{zxx}^M\rangle/\langle\beta_{zzz}^M\rangle$  and  $\langle\beta_{zyy}^M\rangle/\langle\beta_{zzz}^M\rangle$  that results in a small error is rather broad (see the orange region with  $\chi^2 < 8$  in Fig. 2). Combining the data of Ref. [1] with that of other experiments, *e.g.* on electrolyte solutions [26], might allow one to narrow down the uncertainty on  $\langle\beta_{abc}^M\rangle$ . Fig. 1(c) shows directly the agreement between the measured intensity ratio and the results obtained from Eq. 4 using our best estimate for

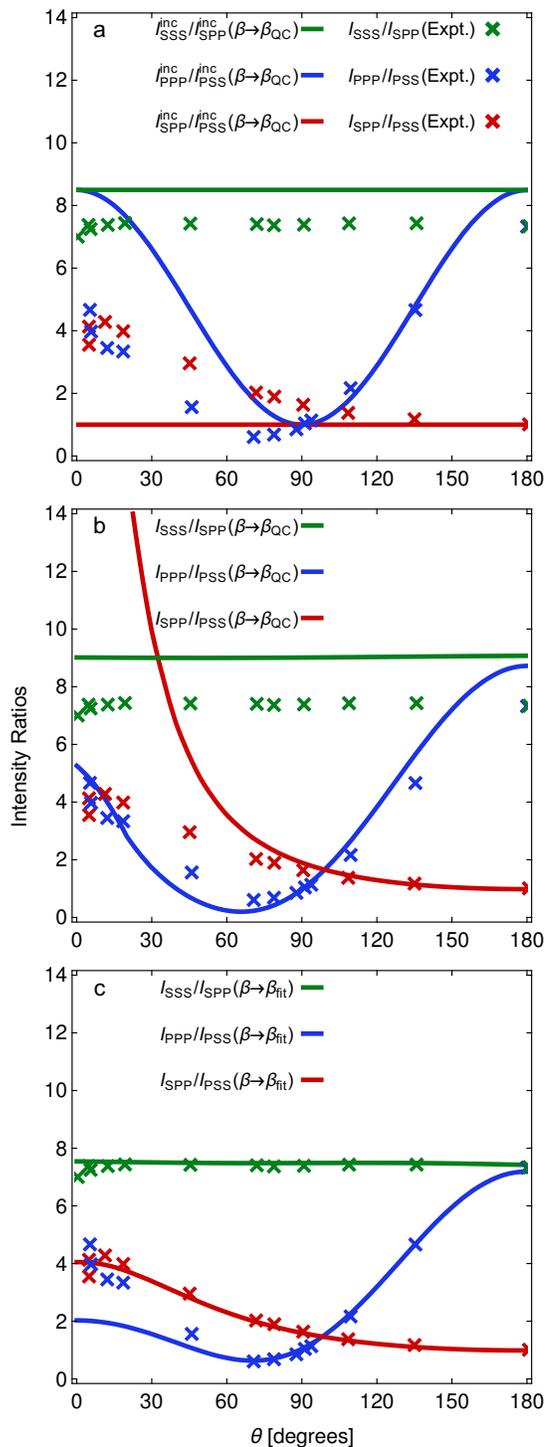


FIG. 1. SHS intensity ratios of bulk water for different polarization combinations as a function of the scattering angle  $\theta$  computed from MD (solid lines) and as measured by Shelton in Ref. [1] (crosses). Intensity ratios with the molecular hyperpolarizability of  $\text{H}_2\text{O}$  in the liquid from Ref. [27] (*i.e.*  $\beta \rightarrow \beta_{\text{QC}}$ ) and (a) assuming incoherent scattering, (b) including also the coherent contribution. (c) Ratios obtained from Eq. 4 including both the incoherent and the coherent contributions and where the molecular hyperpolarizability has been fitted to experiment, *i.e.*  $\beta \rightarrow \beta_{\text{fit}}$ . The nanosecond HRS experimental data is reproduced with permission from the American Institute of Physics from Ref. [1].

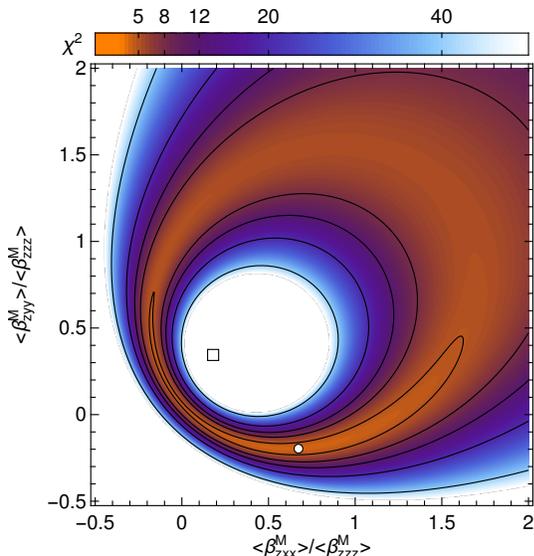


FIG. 2. Contour plot of the mean standard error of the simulated intensity ratios from the experimental data ( $\chi^2$ ) as a function of the independent components of the effective hyperpolarizability of water in the liquid phase. The circle and the square symbol indicate the values of the hyperpolarizabilities that give the minimum in the error and those computed in Ref. [27], respectively.

$\langle \beta_{abc}^M \rangle$ , combined with the structural intermolecular correlations obtained from the MD trajectories. The reason for the discrepancy between the experimental and the simulated intensity ratios in Fig. 1(b) can thus be ascribed to the different value used for the effective hyperpolarizability. Although Fig. 1(c) agrees well with experiments, the agreement is not perfect at low scattering angles. The underlying reason is most likely the fact that the scattering plane becomes ill-defined as  $\theta \rightarrow 0$ , because the two vectors defining this plane ( $\mathbf{k}_{\text{in}}$  and  $\mathbf{k}_{\text{out}}$ , as defined in the SI) become collinear in this limit.

Fig. 3 provides further insight into the correlations probed by SHS experiments. Fig. 3(a) shows a schematic of the experimental system, including for simplicity only a pair of molecules. SHS probes the correlations between projections of unit vectors in the molecular frame onto those of the laboratory reference frame for a given orientation of  $\mathbf{q}$  and combination of  $\mathbf{u}$  and  $\mathbf{v}$ . Fig. 3(a) thus provides a pictorial representation of Eqs.3 and 4. Different components of the  $\langle \mathbf{W}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle$  tensor report on complex combinations of radial and angular correlations. As a concrete example,  $\langle W_{zzzzzz} \rangle$  for the SSS polarization combination, taking an experimental setup in which  $\mathbf{q}$  lies in the  $XY$  plane, is given explicitly by  $\langle \sum_{\alpha, \alpha'} c_{zZ}^3(\alpha) c_{zZ}^3(\alpha') e^{i\mathbf{q} \cdot (\mathbf{r}_\alpha - \mathbf{r}_{\alpha'})} \rangle$ , which involves the pair correlation function of the cube of the molecular dipole's component in the direction of the laboratory  $Z$  axis. Fig. 3(b) shows the effect of these correlations

on three components of  $\langle \mathbf{W}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle$  as a function of wavevector. In the limit as  $q \rightarrow 0$  there is a significant coherent contribution, which is a hallmark of intermolecular correlations.[19] It can be seen that in this limit  $\langle W_{zzzzzz} \rangle$  takes the largest value, while  $\langle W_{zzzzxx} \rangle$  and  $\langle W_{zyzyzy} \rangle$  are about 8 times smaller. This reflects the fact that the correlations between the water dipoles are stronger than those between the  $x$  and  $y$  molecular axes.

In the limit as  $q \rightarrow 0$ ,  $\langle \mathbf{W}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle$  reports on the magnitude of the correlations integrated over all distances. By computing the value of  $\langle \mathbf{W}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle$  at finite  $q$  we can quantify the length scale that gives the largest contribution to the SHS signal. As shown in Figure 3(b),  $\langle W_{zzzzzz} \rangle$  converges to the incoherent limit, oscillating with a period of about  $20 \text{ nm}^{-1}$ , which corresponds to a strong contribution from correlations within the first and second solvation shell of each water molecule. This is shown in more detail by the Fourier transform of  $\langle W_{zzzzzz}(q) \rangle$  into the spatial domain, given in Fig. 3(c). The pair correlation function shown in the figure presents two pronounced peaks, corresponding to the first two solvation shells, and a decays to zero within  $\sim 1 \text{ nm}$ . Therefore, the largest contribution to  $\langle W_{zzzzzz}(q \rightarrow 0) \rangle$  arises from pairs of molecules within the first couple of solvation shells, while long-distance tails give a negligible contribution. Correlations beyond a few nm are not crucial, as is clear from Fig. S2, where it is shown that the intensity ratios differ by a few percent when using a 5 nm simulation box compared to a 20 nm box. The SHS patterns of Shelton [1] have been given a number of different interpretations, all of which involve the role of long-range correlations. Although intermolecular correlations on longer scales may be present, as observed in MD simulations of neat water [37] and in SHS experiments (as well as MD simulations) of electrolyte solutions [26], SHS measurements in neat water can be rationalized in terms of short-range correlations.

Fig. 3(b) focuses on an experimental setup that is particularly simple to interpret. However,  $\langle \mathbf{W}(\mathbf{q}, \mathbf{u}, \mathbf{v}) \rangle$  captures *all* of the correlations that are relevant for an SHS experiment. In the SI (see Figs. S4 and S5) we show the dependence of various tensor elements on the scattering angle and for different polarization combinations. Depending on the geometry of the experiment and the values of  $\langle \beta_{abc}^M \rangle$ , different measurements probe different combinations of molecular correlations. Based on this observation, it is possible to design experiments that are particularly sensitive to a given kind of correlation. For instance, with PPP polarization,  $\theta \approx 0$  and  $\theta \approx 180^\circ$  give the strongest coherent contribution, which is at odds with previous suggestions that measurements should be performed at  $\theta = 90^\circ$ . [16]

Because SHS probes angular intermolecular correlations in liquids, it can be used to gain further insight into the structure of non-centrosymmetric molecular flu-

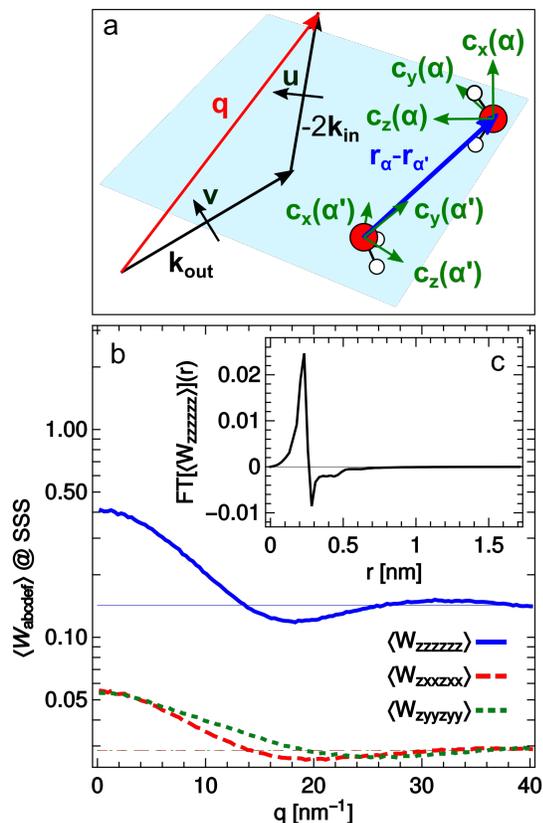


FIG. 3. The role of angular and radial correlations in determining the SHS intensity. (a) Schematic of the SHS system in an arbitrary geometry including for simplicity only a pair of molecules, where  $\mathbf{q}$ ,  $\mathbf{k}_{\text{in}}$ ,  $\mathbf{k}_{\text{out}}$   $\mathbf{u}$  and  $\mathbf{v}$  define the experimental setup, while the  $\mathbf{c}$  vectors are the unit vectors of molecule  $\alpha$  and  $\alpha'$  in their respective reference frames. (b) Wave vector dependence of  $\langle W_{zzzzzz} \rangle$ ,  $\langle W_{zxxxxx} \rangle$  and  $\langle W_{zyyzyy} \rangle$  tensor elements in the SSS polarization (thin lines are the incoherent parts of these tensors). (c) Fourier transform of  $\langle W_{zzzzzz} \rangle(q)$  demonstrating the short-range nature of the correlations that contribute to SHS.

ids in addition to the more widely used X-ray and neutron scattering, which are mostly sensitive to radial intermolecular correlations [38–40]. While there have been extensive computational investigations of X-ray scattering experiments, the simulation of SHS experiments has received rather limited attention [41]. Previous experiments have been analyzed under the assumption of an incoherent SHS intensity [12, 14, 16, 18, 20, 32]. For instance, under this assumption the hyperpolarizability of several solute molecules in the condensed phase has been extracted [18]. Based on the developments presented here, it is now also possible to analyze the signal from the solvent, without assuming that the scattering process is incoherent, and being able to evaluate the SHS intensity for arbitrary scattering angle, polarization combination and wave vector. Furthermore, separating the molecular hyperpolarizability  $\langle \beta_{abc}^M \rangle$  and the

structural term  $\langle W_{abcdef} \rangle$  in 4 makes it possible to disentangle the role of the second order optical response in the liquid from that of the intermolecular correlations, thereby allowing for a more thorough connection to experiments, and for an unbiased assessment of the most relevant length scales. An important question for future work would be, for instance, to investigate ionic solutions in order to evaluate the nature and length scales of the intermolecular water-water correlations that underlie the results of Ref. [26].

In conclusion, we have developed a method that can be used in atomistic computer simulations of liquids to calculate the second harmonic scattering intensity, and which fully accounts for the coherent contribution to the scattering due to interactions between molecules. The method also provides a way to extract an effective molecular hyperpolarizability in the liquid phase, without having to rely on an over-simplified representation of the complex local environment of a water molecule [27, 34, 42]. By applying this method to nanosecond HRS experiments of liquid water [1] we have shed light onto their coherent nature. We have also provided deep insights into the radial and angular correlations probed by these experiments, showing that the angular dependence of the SHS signal can be explained in terms of inter-molecular correlations on a length scale of the order of 1 nm. The main assumption made in this work is that nanosecond SHS experiments can be described in terms of an effective molecular hyperpolarizability  $\langle \beta_{abc}^M \rangle$ . Work is currently underway to go beyond this treatment, by characterizing the dependence of  $\beta_{abc}^M$  on the molecular environment, and thereby assessing the role of fluctuations. Overall, we hope that these developments will stimulate the use of molecular simulations to aid the interpretation of SHS experiments in more complex bulk liquids and at aqueous interfaces.

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## SUPPORTING INFORMATION

The Supporting Information contains further details of the following aspects: the geometrical setup of the SHS experiments; the computational details of the MD simulations; a discussion on the convergence of the SHS simulations at low scattering wavevectors; a discussion of the effect of finite-size systems and of different water force-field on the computation of the intensity ratios.

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